

Probabilistic Bug Localization for Analog/Mixed-Signal Circuits using Probabilistic Graphical Models

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Outline

- Overview
- Bug localization using graphical models
 - Graphical model creation
 - Gaussian Bayesian network
 - Table-based Bayesian network
 - Bug localization by statistical inference
- Experimental results
- Conclusion

Problem: Time-Consuming Debugging

- Debugging tasks are major bottlenecks in IC design
 - Mostly depends on trial-and-errors
 - Takes a significant amount of time!

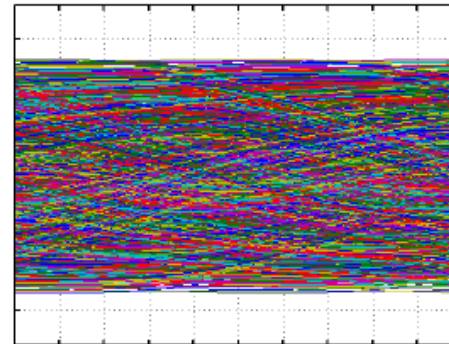
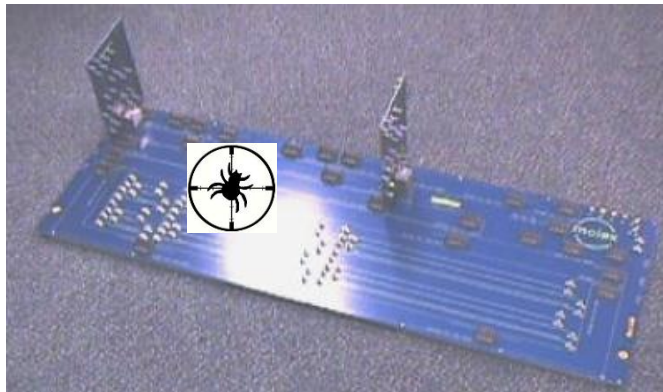
Return to Zero



EEWeb.com

Goal: Automatic Bug Localization

- Goal is to develop a tool that can automatically localize bugs from available waveforms and models, primarily for **post-silicon validation**



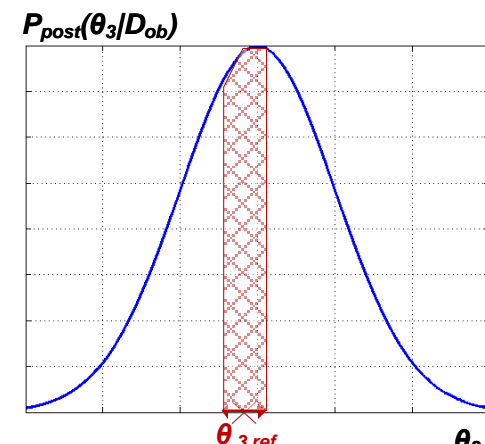
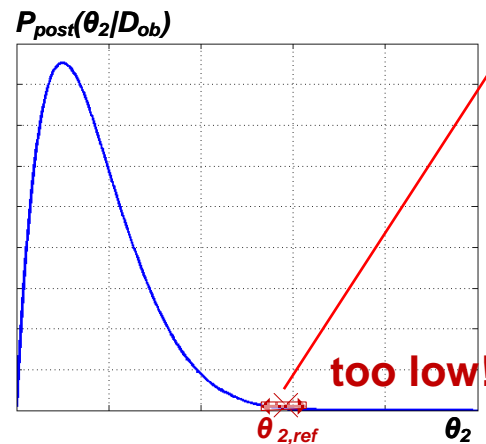
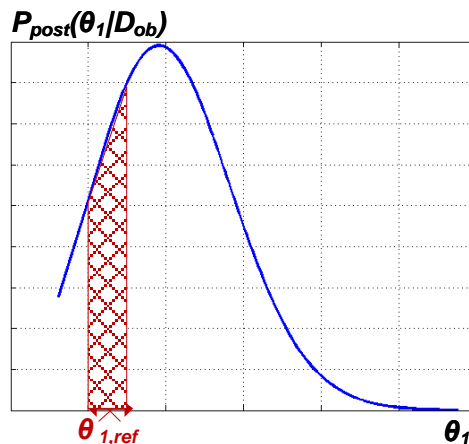
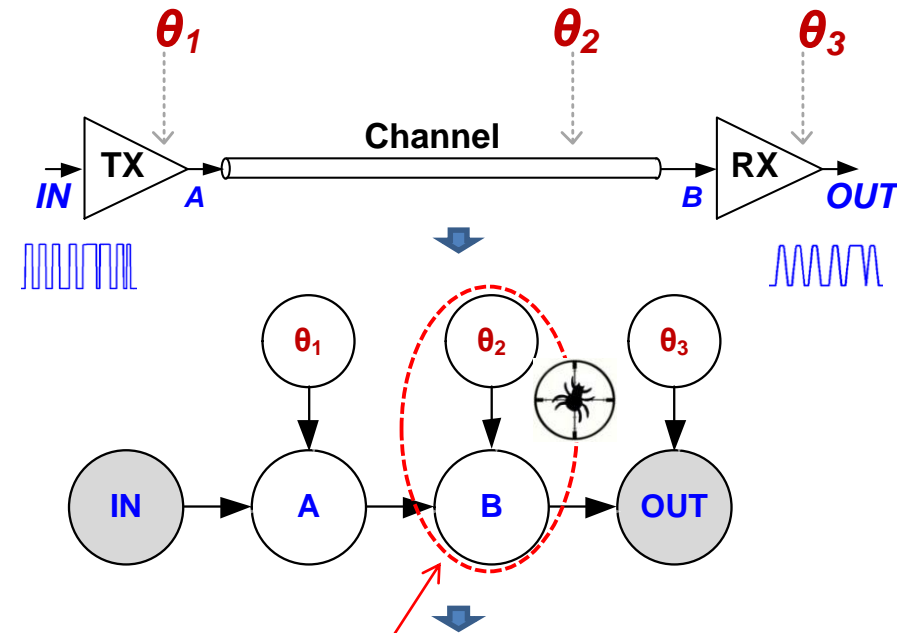
Closed eye, Failure!

Which block caused this failure ?



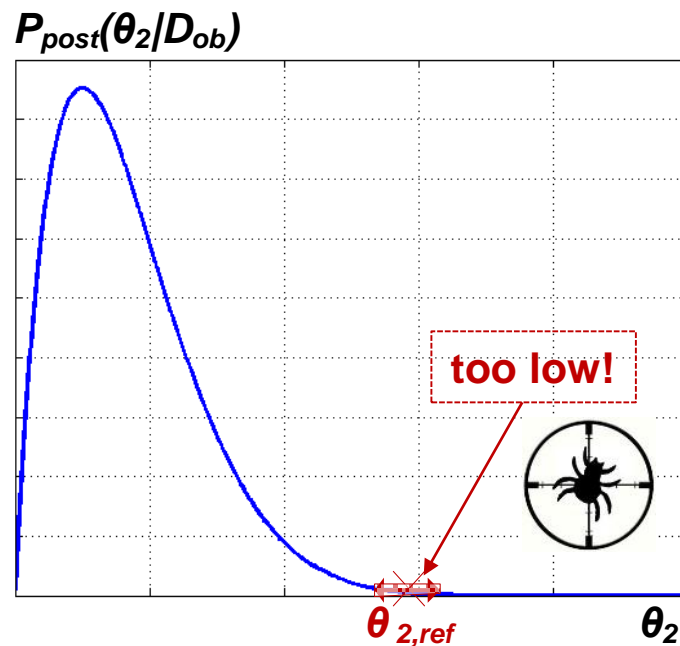
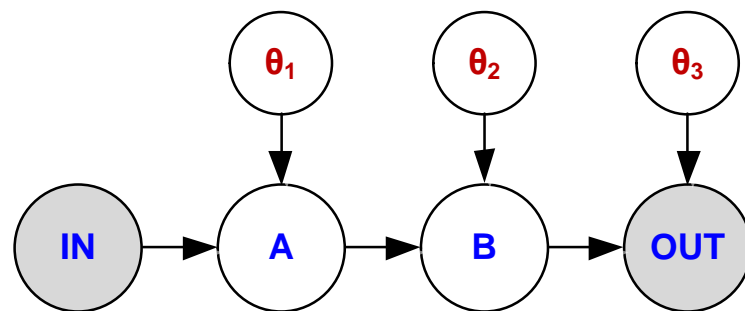
Proposed Approach: Bug Diagnosis Using Probabilistic Graphical Models

1. Construct probabilistic graphical model
2. Make an observation
3. Estimate the posterior probability of a system's parameter θ
4. If $P_{\text{post}}(\theta \text{ in } \theta_{\text{spec_range}}) < \text{threshold}$, θ and its associated sub-block are reported as failure root-causes
 - If multiple bug root-causes are found, rank them according to $P(\theta = \theta_{\text{ref}} | D_{\text{ob}})$



Advantages of Our Approach

- Uncertainty/noise can be modeled
- Non-linearity can be modeled
- Efficient inference algorithms exist

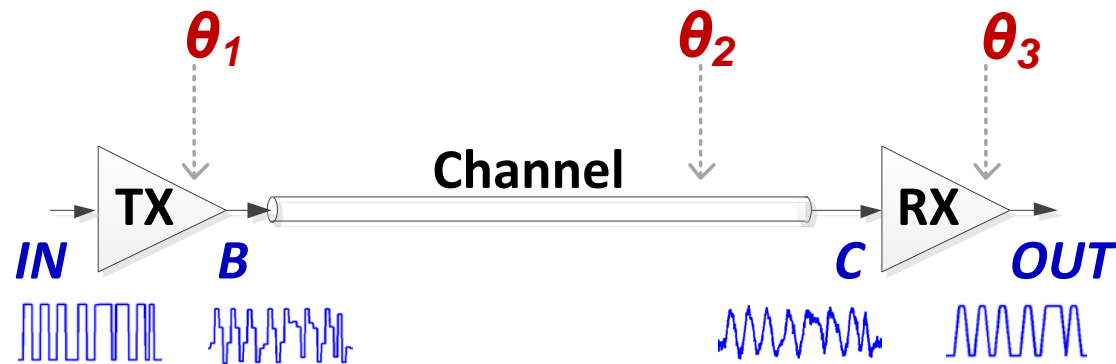


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Probabilistic Models

- A system's behavior can be described by *probability* instead of a *functional* relationship



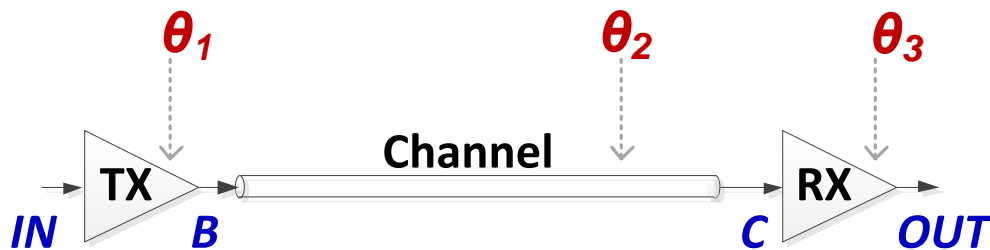
$$P(IN, B, C, OUT, \theta_1, \theta_2, \theta_3)$$



This is difficult to characterize!

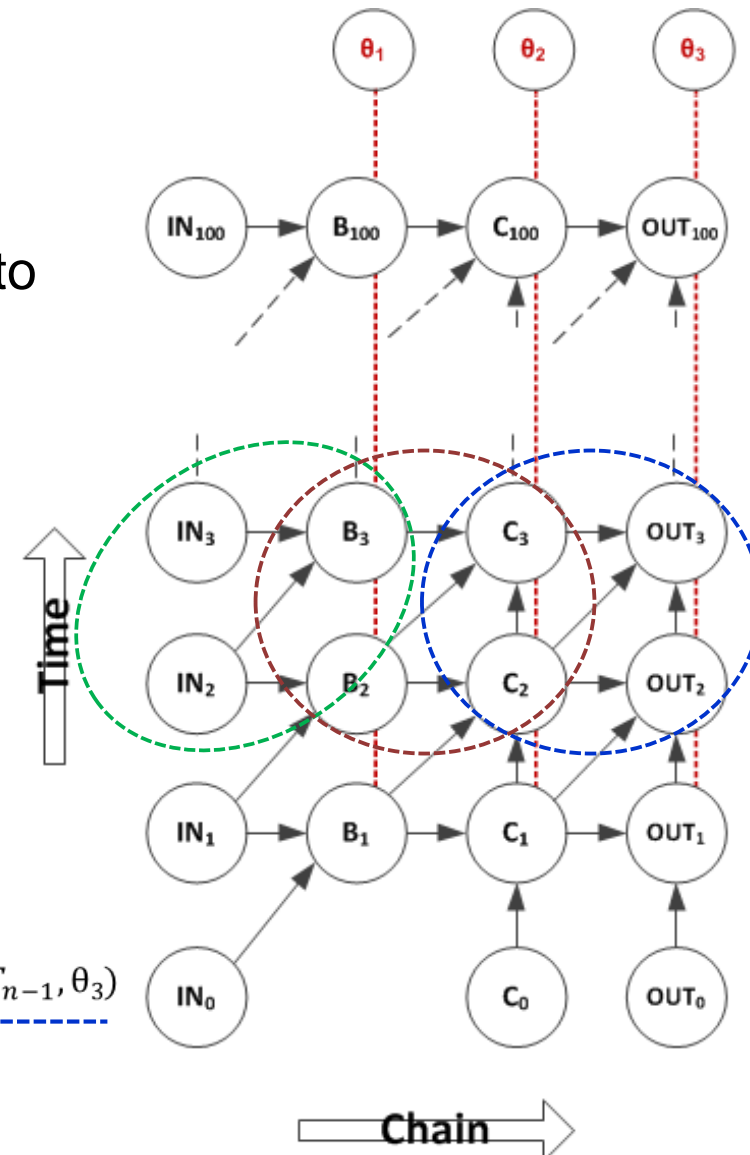
Probabilistic Graphical Model

- We can significantly reduce the complexity ***by graphical model***
 - Can decompose a full joint distribution into small factors



$$P(IN_{t:1}, B_{t:1}, C_{t:1}, OUT_{t:1}, \theta_1, \theta_2, \theta_3)$$

$$= \prod_{n=1}^{100} \underbrace{P(IN_n)}_{\text{green dashed line}} \underbrace{P(B_n | IN_{n-1:n}, \theta_1)}_{\text{green dashed line}} \underbrace{P(C_n | B_{n-1:n}, C_{n-1}, \theta_2)}_{\text{red dashed line}} \underbrace{P(OUT_n | C_{n-1:n}, OUT_{n-1}, \theta_3)}_{\text{blue dashed line}}$$



Two Parametric Model of Factors in Graphical Model

- Conditional Probability Density (CPD)

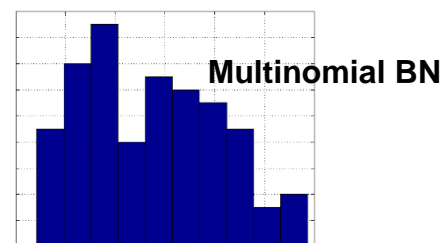
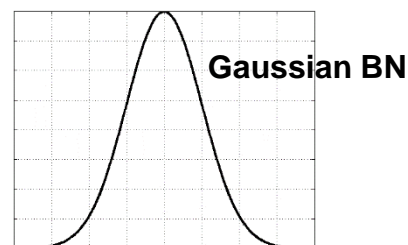
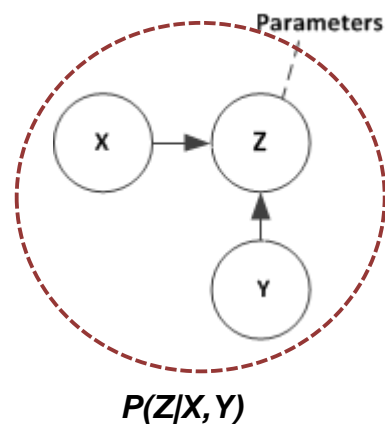
- A template to describe CPD, $P(\mathbf{Z}_{out} | \mathbf{X}_{in}, \mathbf{Y}_{in})$

- Gaussian Bayesian network (GBN)

- $P(Z | X, Y) \sim \text{Normal}(aX + bY, \sigma^2)$
 - For **linear** block

- Table-based Bayesian network (TBN)

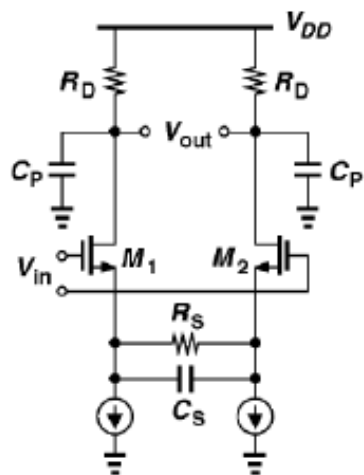
- $P(Z | X, Y) \sim \text{Multinomial}(p_1, p_2, \dots, p_k)$
 - For **nonlinear** block



Gaussian Bayesian Network (GBN) Model

Example – Continuous Time Linear Equalizer

- CTLE example



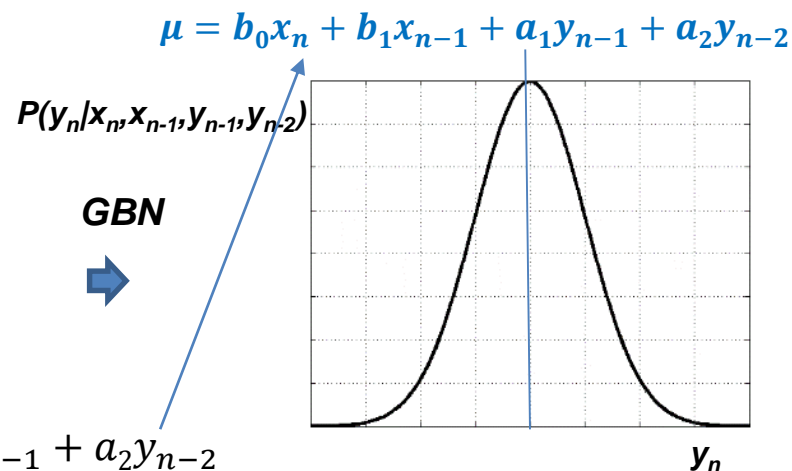
Discrete-time



$$H(z) = K \frac{b_0 + b_1 z^{-1}}{1 + a_1 z^{-1} + a_2 z^{-2}}$$

$$y_n = b_0 x_n + b_1 x_{n-1} + a_1 y_{n-1} + a_2 y_{n-2}$$

GBN



$$H(s) = \frac{g_m}{C_p} \frac{(s + \frac{1}{R_s C_s})}{(s + \frac{1 + \frac{g_m R_s}{2}}{R_s C_s})(s + \frac{1}{R_D C_p})}$$

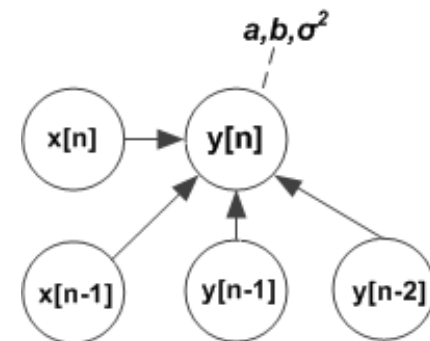
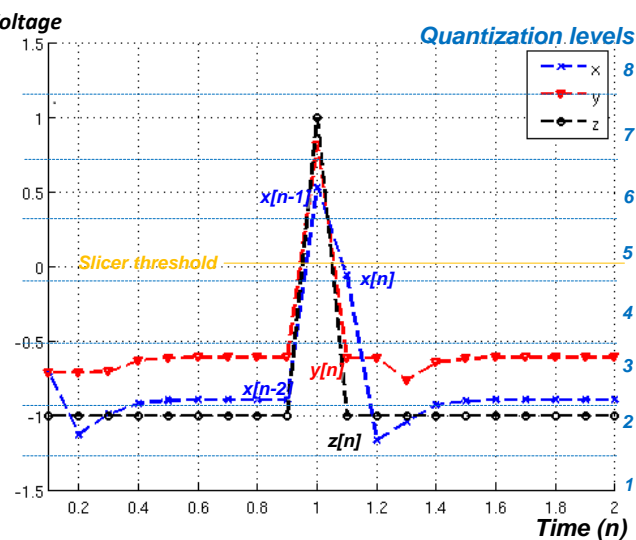
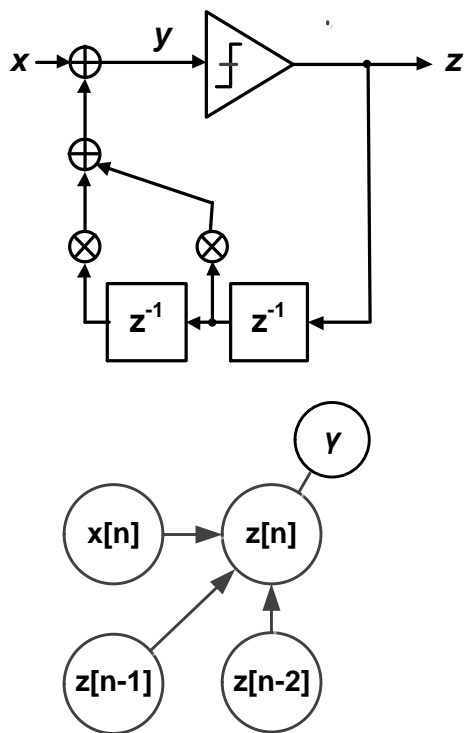
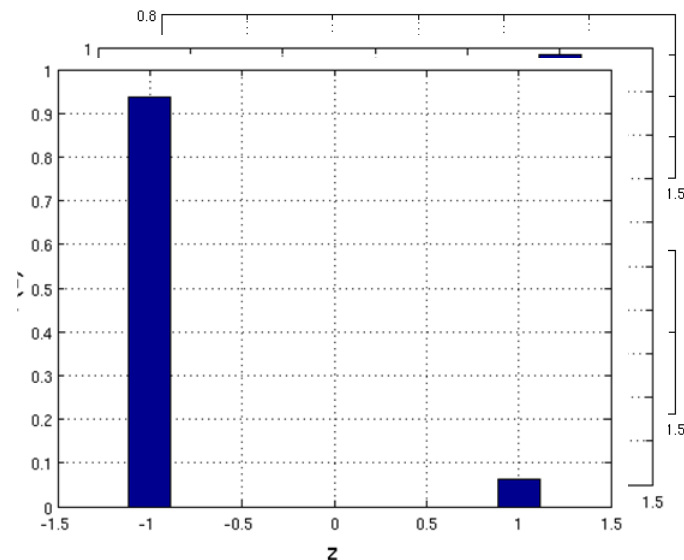


Table-Based Bayesian Network (TBN) Model Creation – Decision Feedback Equalizer

■ DFE example



$x[n]$ =input
 $y[n]$ =slicer's input
 $z[n]$ =output



$P(y[n]|x[n]=5, z[n-1]=1, z[n-2]=-1)$
 $P(y[n]|x[n]=6, z[n-1]=-1, z[n-2]=-1)$
 $P(y[n]|x[n]=3, z[n-1]=-1, z[n-2]=-1)$

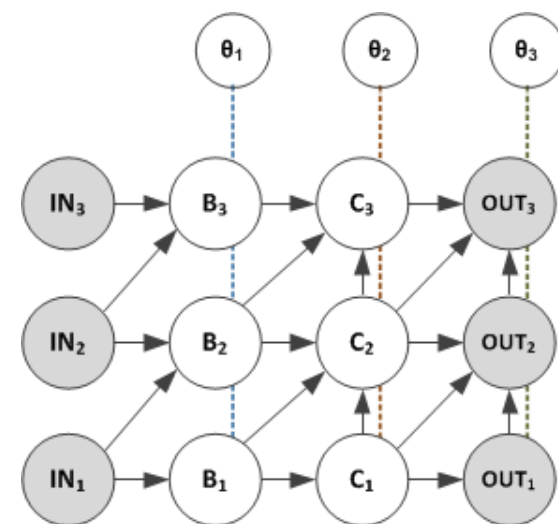
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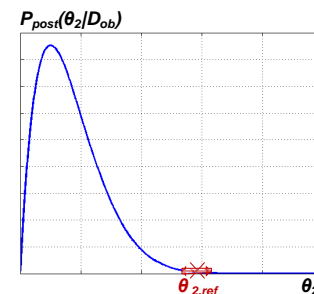
Bug Localization by Statistical Inference:

Computing $P_{\text{posterior}}(\theta \mid D_{\text{ob}})$

- We want to estimate the probability of a parameter (θ) after observation (D_{ob}) by statistical inference
- Possible Approaches
 - Exact inference
 - Junction tree algorithm
 - Approximate inference
 - ***Gibbs sampling***



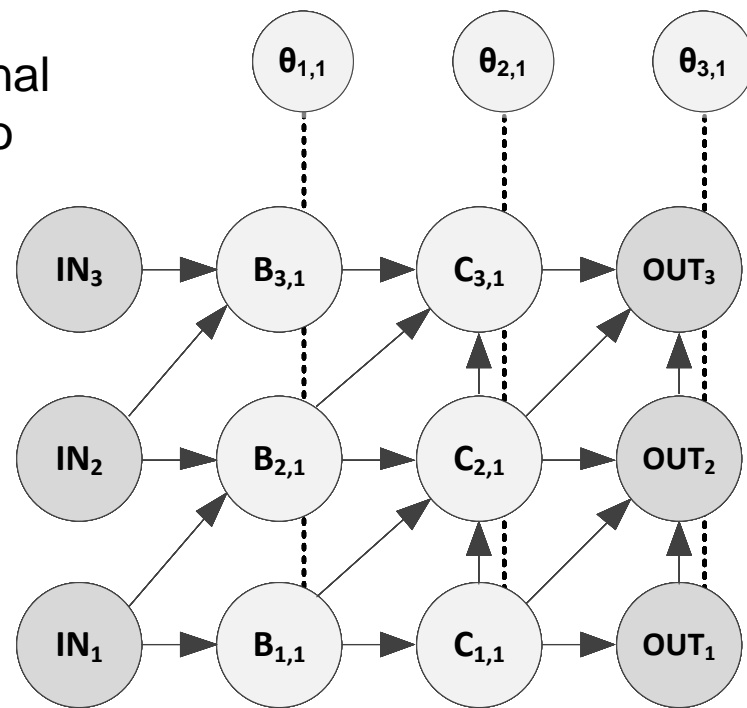
How do we get $P_{\text{posterior}}(\theta \mid D_{\text{ob}})$?



Statistical Inference by Gibbs Sampling: Computing $P_{\text{posterior}}(\theta \mid D_{\text{ob}})$

- **Gibbs Sampling** can be used when the conditional distribution of each variable is known and is easy to sample from

1. Start with an initial guess $X_0 = (B_{1,0}, B_{2,0}, \dots, \theta_{3,0})$
2. Take a sample $B_{1,1}$ from $P(B_1 \mid B_{2,0}, B_{3,0}, \dots, \theta_{3,0})$ and update B_1
3. Take samples for B_2 to B_3 and update them
4. Take a sample $\theta_{1,1}$ from $P(\theta_1 \mid B_{1,0}, \dots, \theta_{2,0}, \theta_{3,0})$ and update θ_1
5. Take samples for C_1 to C_3 and update them
6. Take samples θ_2 to θ_3 and update them
7. Iterate 2~6 step N times
8. Estimate $P_{\text{post}}(\theta \mid D_{\text{ob}}) \sim \text{Histogram}(\text{Samples})$
 - $P(\theta_1 \mid D_{\text{ob}}) \sim \text{Histogram}(\theta_{1,k+1}, \theta_{1,k+2}, \dots, \theta_{1,k+N})$



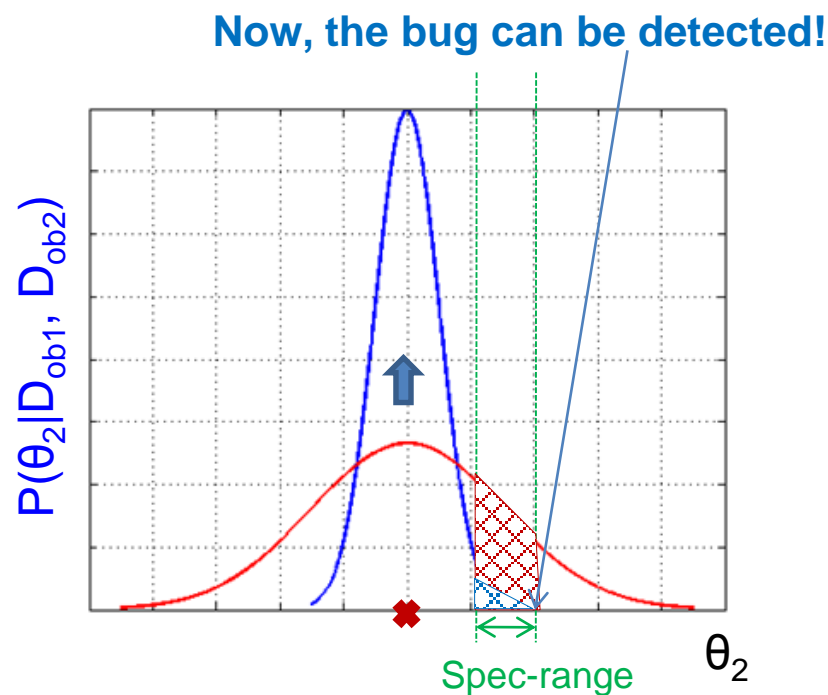
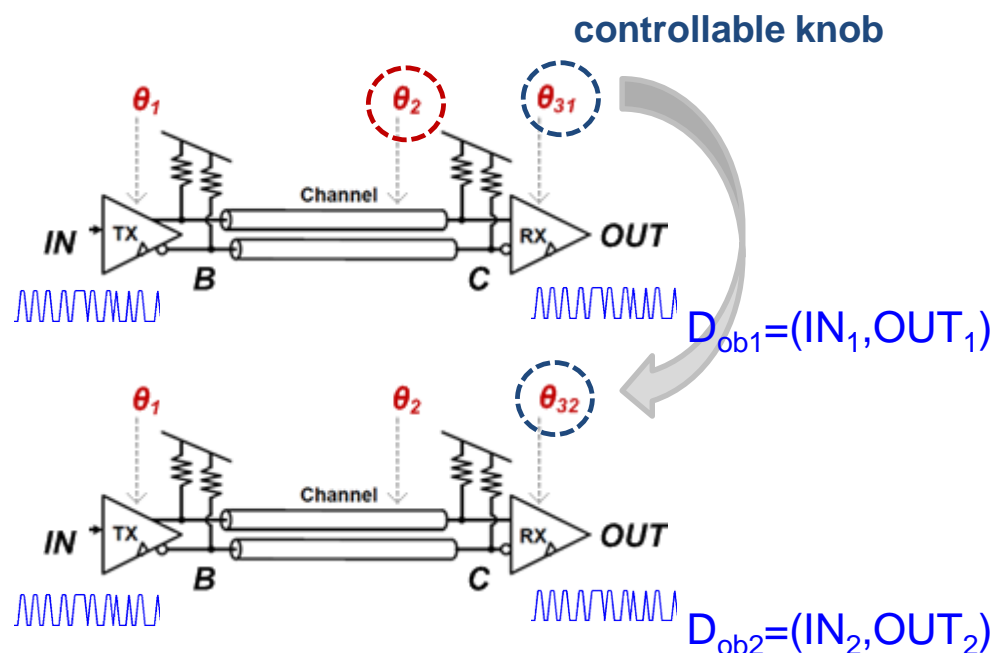
$(B_{1,1}, B_{2,1}, \dots, C_{1,1}, C_{2,1}, \dots, \theta_{3,1})$

$(B_{1,2}, B_{2,2}, \dots, C_{1,2}, C_{2,2}, \dots, \theta_{3,2})$

\dots
 $(B_{1,N}, B_{2,N}, \dots, C_{1,N}, C_{2,N}, \dots, \theta_{3,N})$

Increasing Accuracy by Using Controllability

- The method may miss a bug root-cause due to highly **limited observability**
- However, we can increase accuracy and differentiate bug root-causes by using **controllability**



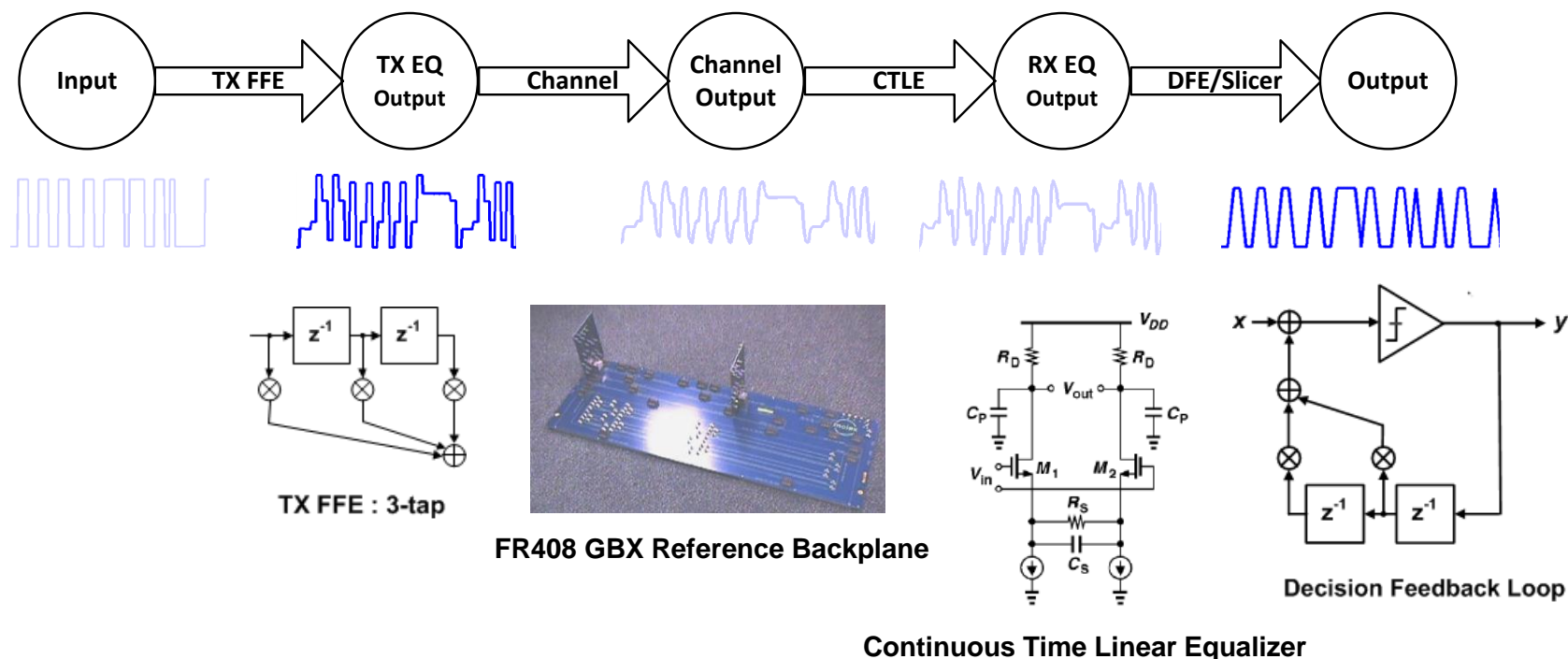
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Test Case – A 5 Gbps I/O Link

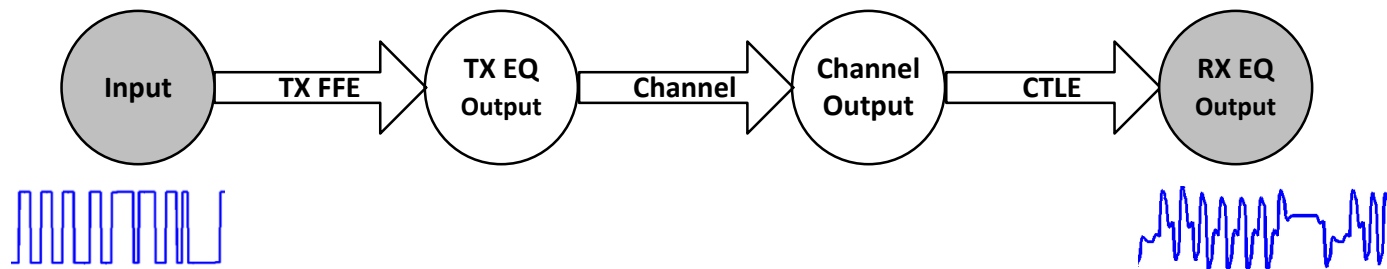
■ System Parameters (θ)

- TX FFE, Channel, RX CTLE : pole / zero
- DFE: tap coefficients / slicer threshold



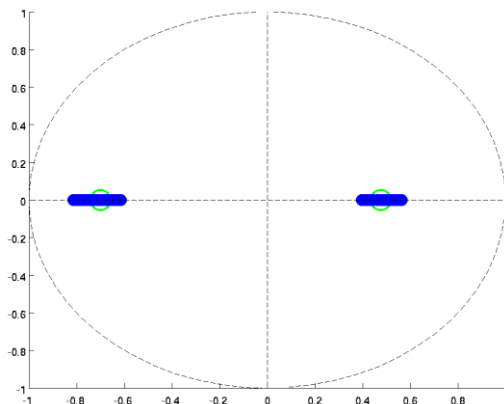
Experiment (1) – The Posteriors Cover True Parameters As Expected

- Posterior distributions of FFE, channel and CTLE parameters and true parameter locations

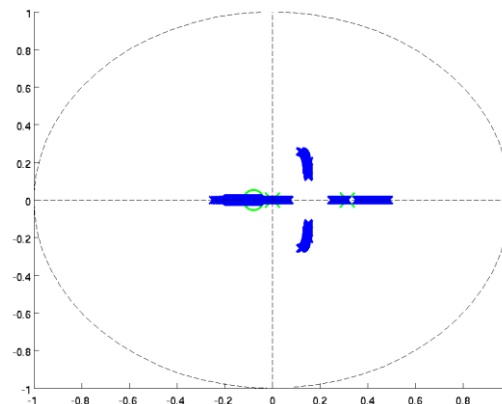


True pole/zero location (x / o)

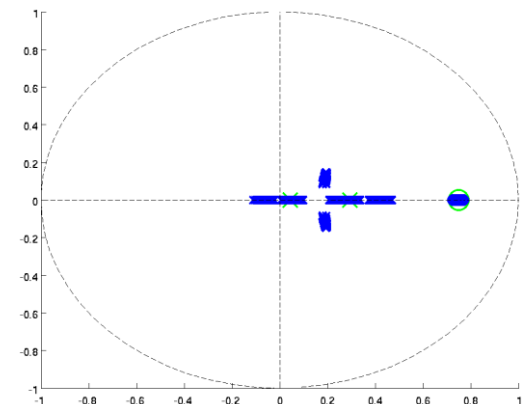
Estimated posterior distribution of pole/zero (x / o)



Zero map of TX FFE



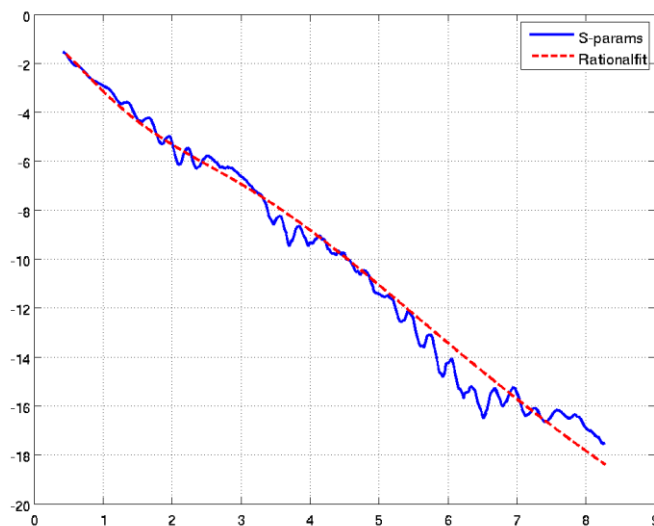
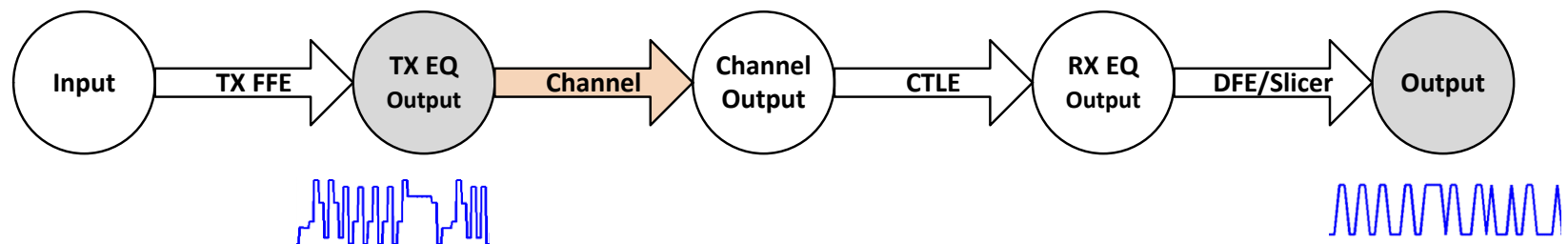
Pole/Zero map of channel



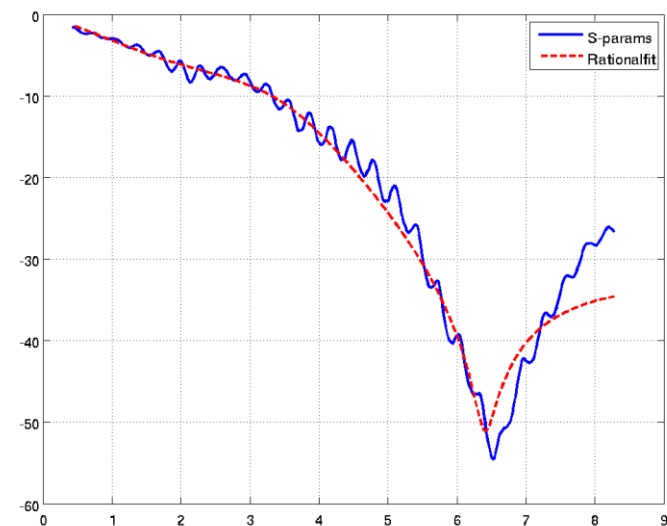
Pole/Zero map of CTLE

Experiment (2) – The Problematic Buggy Channel Can be Identified

- In this experiment, a channel is replaced by a problematic lossy channel

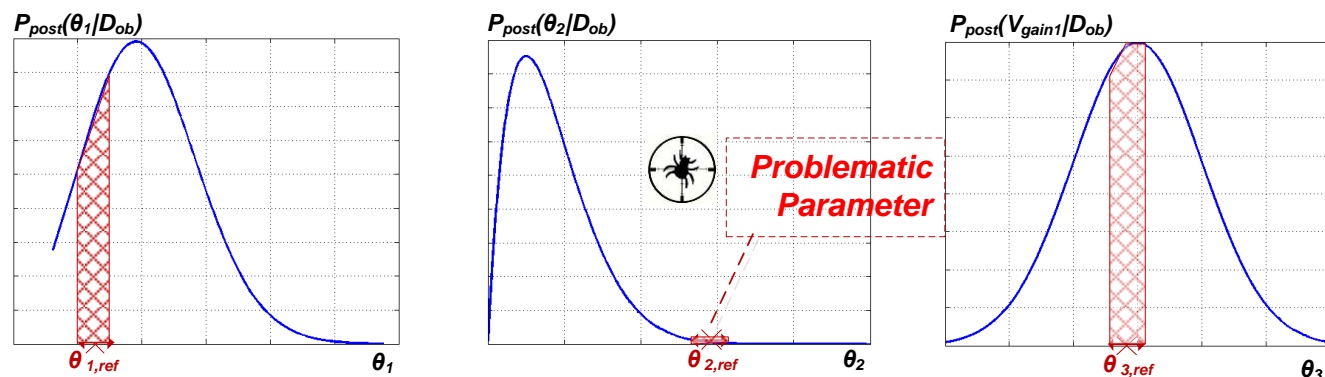
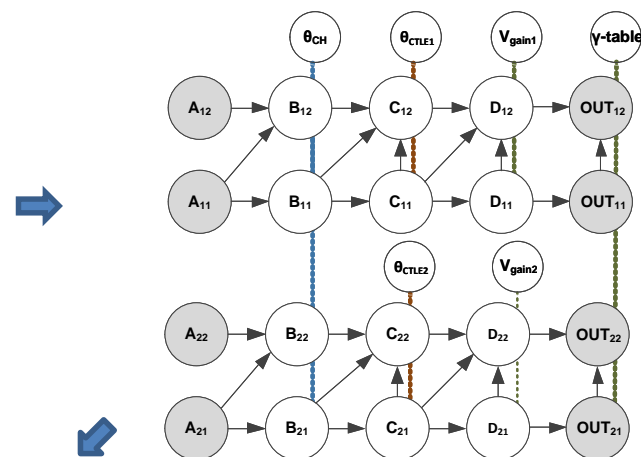
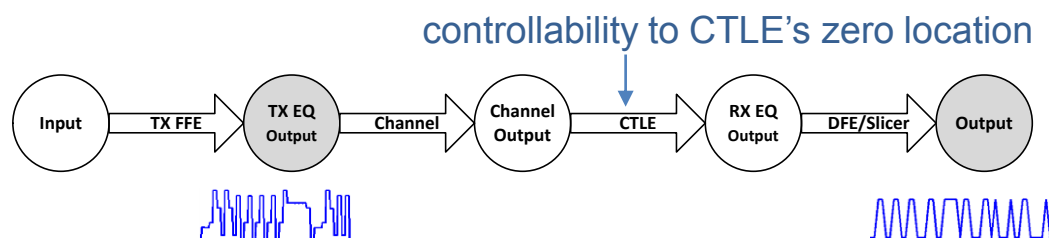


Frequency response of **desired** channel



Frequency response of **lossy** channel

The Bug Localization and Ranking Procedure

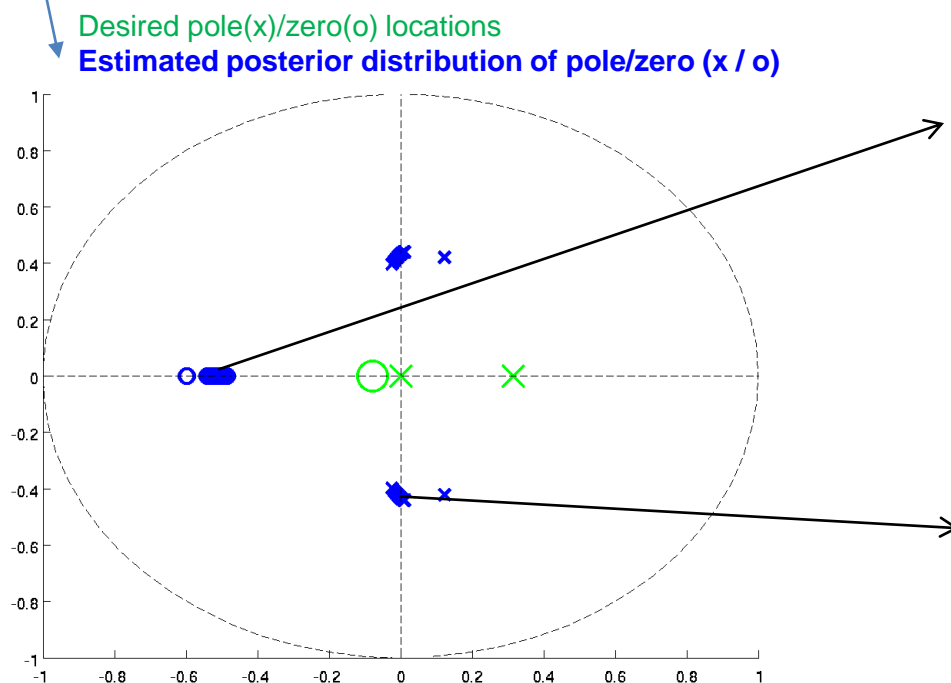


Ranking

- Rank them according to $P(\theta \text{ in } \theta_{\text{spec}} | D_{\text{ob}})$
- $P(\theta_2 \text{ in } \theta_{2,\text{spec}} | D_{\text{ob}}) < P(\theta_1 \text{ in } \theta_{1,\text{spec}} | D_{\text{ob}}) < \dots$
- Rank in order of $\theta_2, \theta_1, \dots$

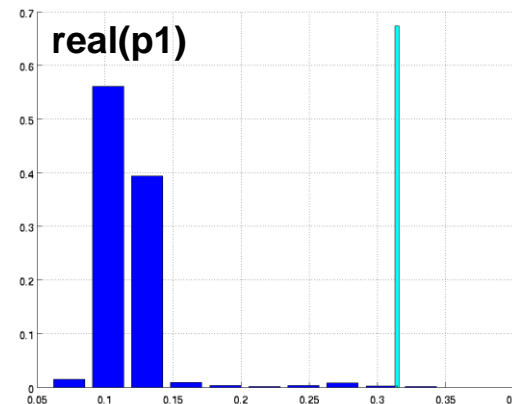
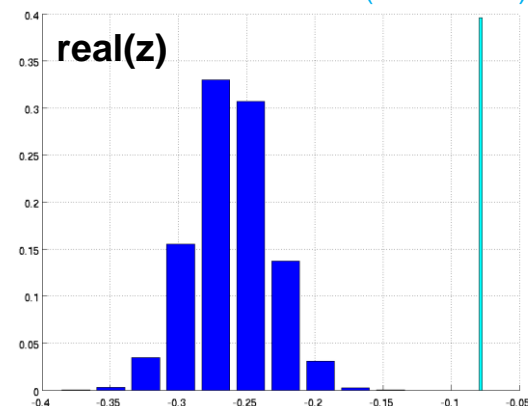
Experiment (2) – A Buggy Lossy Channel is Identified As the Bug Root-Cause

$P_{post}(\theta \text{ in } \theta_{spec})$	Real(z1)	Imag(z1)	Real(p1)	Imag(p1)	Real(p2)	Imag(p2)
Channel	0.17%	100%	1.7%	5.4%	15%	5.4%
CTLE	65%	100%	58%	90%	63%	90%



Estimated parameter posterior of buggy channel

Desired Parameter Value (Narrow bar)



Conclusion

- Under limited observability, the proposed bug method can automatically localize bugs
 - Nonlinearity and uncertainty could be well reflected
 - Can leverage controllability
 - Can rank multiple bug root-causes

